

# Advanced Pattern Block Book

## Answer Key

### 1.1 Quadrilateral Force-Out (page 3)

Check students' work.

### 1.2 Star Time (page 5)

Check students' work.

### 1.3 Gretles (page 7)

1. No
2. No
3. Yes
4. Yes

### 1.4 Cover Three (page 9)

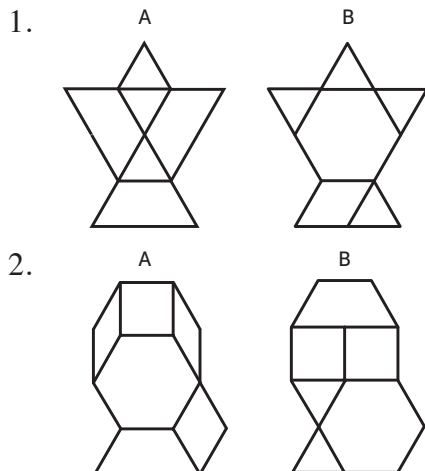
Check students' work.

### 1.5 Towering Hexagons (page 11)

Check students' work.

### 1.6 Take Six (page 13)

Answers will vary. Sample answers:

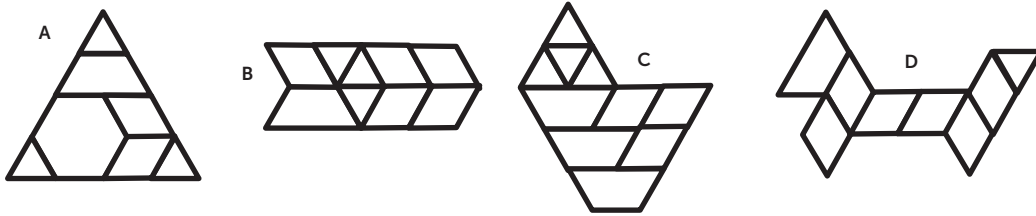


### 1.7 Countdown 10, 9, 8, ...1! (page 15)

Check students' work.

### 1.8 Hidden Wonders (page 17)

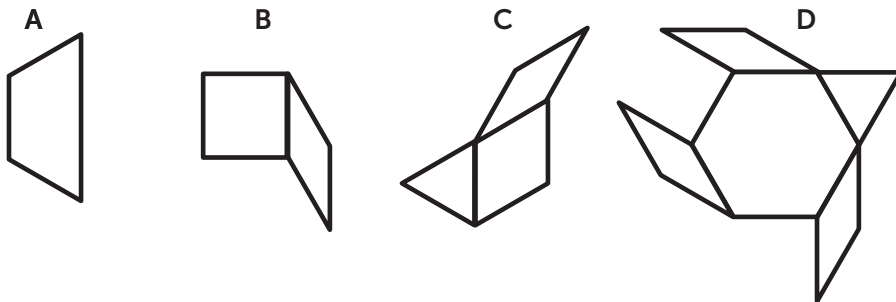
Arrangements will vary. Sample answers:



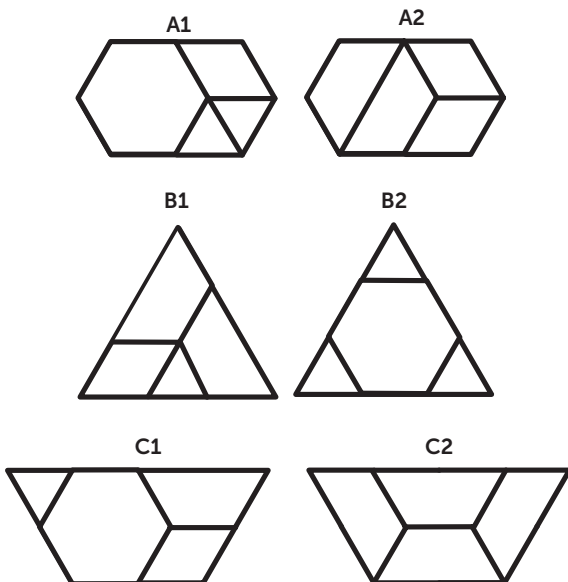
### 1.9 Both Sides Now (page 19)

Check students' work.

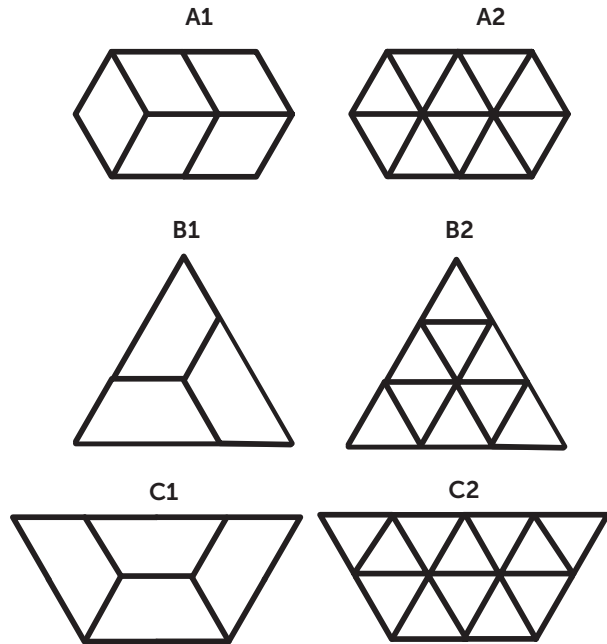
### 1.10 Asteroids (page 21)



### 2.1 Any Four (page 25)



## 2.2 The Same Block (page 27)



## 2.3 Only One Color (page 29)

Sled:

Block	Guess	Count	Fraction Name
blue rhombus	will vary	7	1/7
triangle	will vary	14	1/14

Cup:

Block	Guess	Count	Fraction Name
blue rhombus	will vary	9	1/9
triangle	will vary	18	1/18

Kite:

Block	Guess	Count	Fraction Name
blue rhombus	will vary	9	1/9
trapezoid	will vary	6	1/6

## 2.4 Space Station (page 31)

Check students' work.

## 2.5 Fraction Names (page 33)

- A. Check students' work.
- B.  $1/2$ ;  $1/3$ ;  $1/6$ 
  - 1. Example: Answer given
  - 2.  $4/6$  or  $2/3$  shaded;  $2/6$  or  $1/3$  unshaded
  - 3.  $1/3$  shaded;  $2/3$  unshaded
  - 4.  $3/6$  or  $1/2$  shaded;  $3/6$  or  $1/2$  unshaded
  - 5.  $2/3$  shaded;  $1/3$  unshaded

## 2.6 Just One (Hexagon)! (page 35)

- 1.  $2$ ;  $1/2$
- 2.  $3$ ;  $1/3$
- 3.  $6$ ;  $1/6$
- 4. Example: Answer given.
- 5. 1 triangle;  $1/6$
- 6. 1 rhombus;  $1/3$
- 7. 1 trapezoid;  $1/2$
- 8. 1 blue rhombus;  $1/3$
- 9. 1 trapezoid;  $1/2$
- 10. 1 blue rhombus;  $1/3$
- 11. 1 triangle;  $1/6$
- 12. 1 blue rhombus;  $1/3$
- 13. 1 triangle;  $1/6$

## 2.7 Cover with One Color (page 37)

- A. Example: Answer given.
- B.  $1/6 + 1/6 + 1/6 = 3/6$  or  $1/2$
- C.  $1/2 + 1/2 = 1$
- D.  $1/2 + 1/6 = 4/6$  or  $2/3$
- E.  $1/6 + 1/3 = 3/6$  or  $1/2$
- F.  $1/6 + 1/6 + 1/6 + 1/6 = 4/6$  or  $2/3$

## 2.8 The Missing Piece (page 39)

1. Example: Answer given.
2. blue rhombus,  $\frac{1}{6}$  OR 2 triangles,  $\frac{2}{12}$  or  $\frac{1}{6}$
3. 2 blue rhombuses,  $\frac{1}{3}$  OR 4 triangles,  $\frac{4}{12}$  or  $\frac{1}{3}$
4. hexagon,  $\frac{1}{2}$
5. hexagon,  $\frac{1}{2}$
6. trapezoid,  $\frac{1}{4}$

## 2.9 Some Sum! (page 41)

1.  $\frac{1}{6}$
2.  $\frac{3}{4}$
3. 1 triangle + 1 blue rhombus = 1 trapezoid =  $\frac{1}{4}$
4. 1 blue rhombus + 2 blue rhombuses = 1 hexagon =  $\frac{1}{2}$
5. 4 triangles + 1 blue rhombus = 1 hexagon =  $\frac{1}{2}$
6. 1 trapezoid + 3 blue rhombuses = 3 trapezoids =  $\frac{3}{4}$

## 2.10 Changing Values (page 43)

Top: hexagon is  $\frac{1}{2}$ ; trapezoid is  $\frac{1}{4}$ ; blue rhombus is  $\frac{1}{6}$ ; triangle is  $\frac{1}{12}$

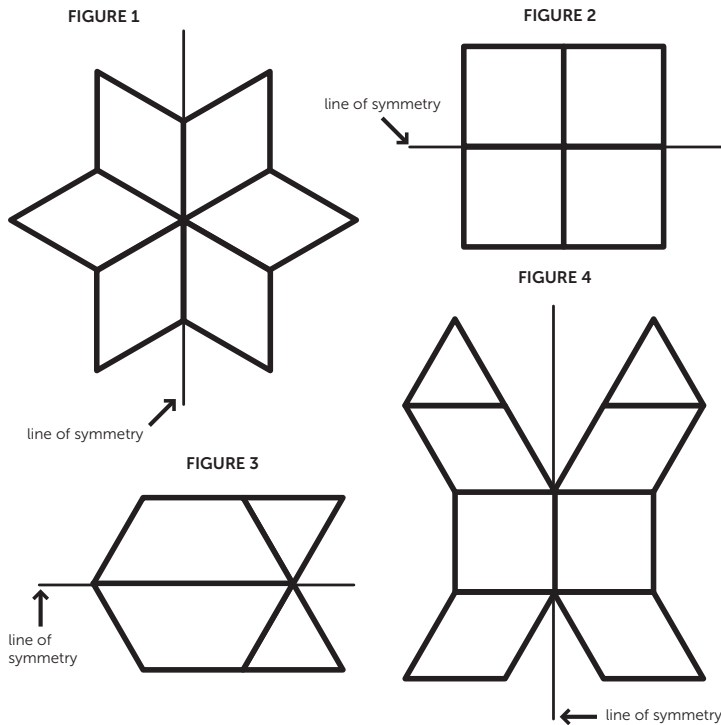
1. Example: Answer given.
2.  $\frac{1}{6} + \frac{1}{6} + \frac{1}{6} = \frac{1}{2}$
3.  $\frac{1}{2} + \frac{1}{4} = \frac{3}{4}$
4.  $\frac{1}{12} + \frac{1}{12} + \frac{1}{6} = \frac{1}{3}$
5.  $\frac{1}{4} + \frac{1}{12} + \frac{1}{6} = \frac{1}{2}$
6.  $\frac{1}{4} + \frac{1}{12} + \frac{1}{12} = \frac{5}{12}$
7.  $\frac{1}{6} + \frac{1}{12} = \frac{1}{4}$
8.  $\frac{1}{6} + \frac{1}{6} + \frac{1}{12} + \frac{1}{12} = \frac{1}{2}$

## 3.1 Which Block? (page 47)

1. A. trapezoid  
B. blue rhombus or tan rhombus  
C. hexagon

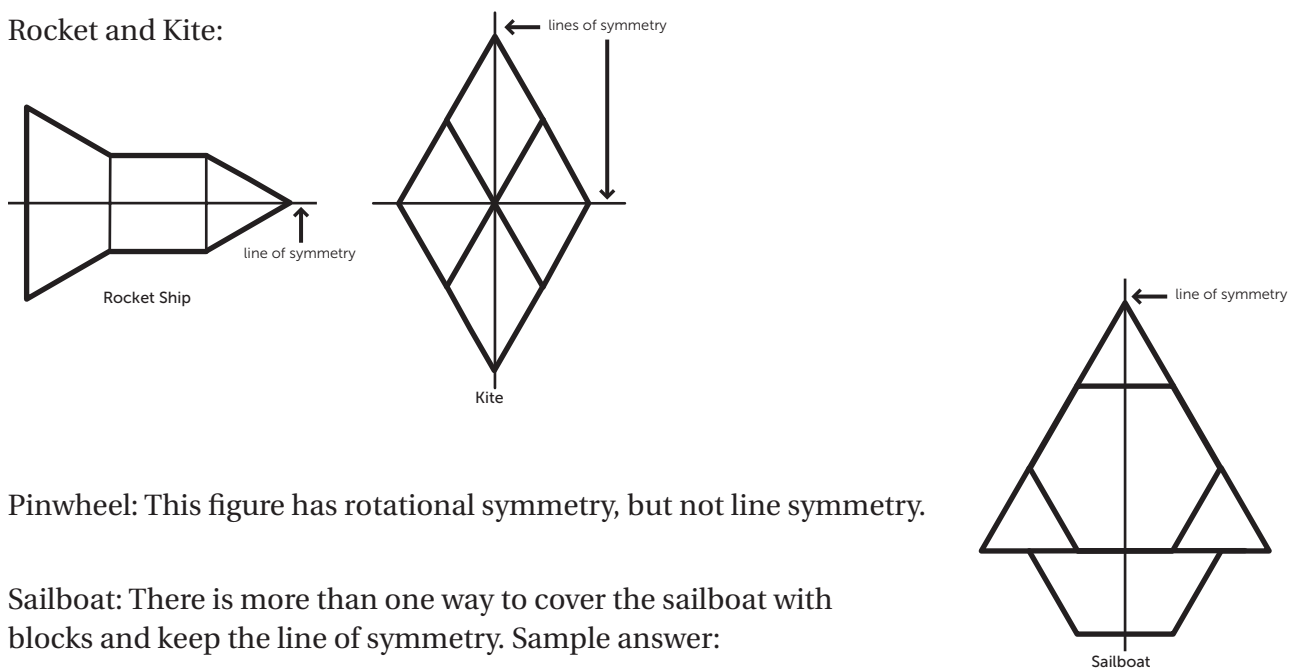
- 2. Maggie: triangle
- Bill: tan rhombus
- Vincent: red trapezoid
- Sandi: blue rhombus

### 3.2 Folded Shapes (page 49)



### 3.3 Simple Symmetry (page 51)

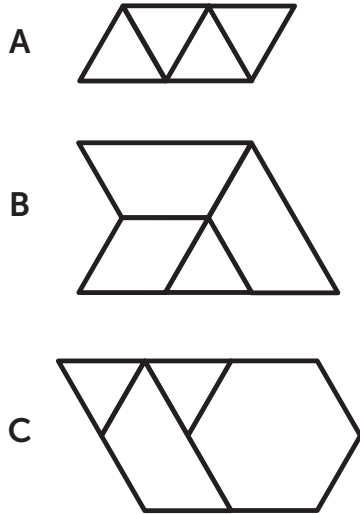
Rocket and Kite:



Pinwheel: This figure has rotational symmetry, but not line symmetry.

Sailboat: There is more than one way to cover the sailboat with blocks and keep the line of symmetry. Sample answer:

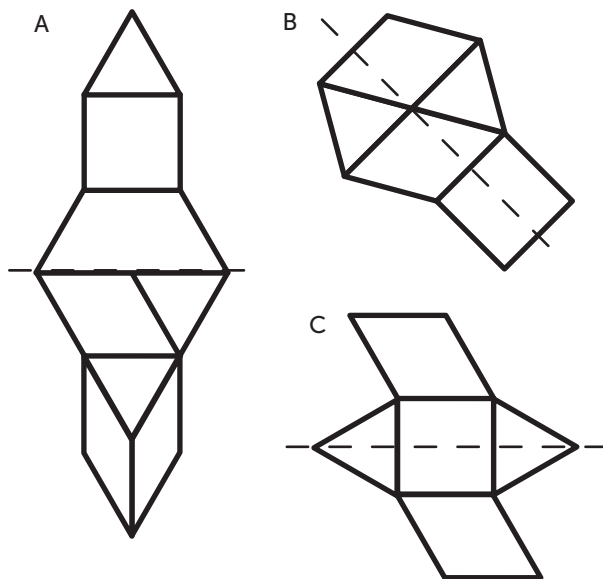
### 3.4 Copy Cat (page 53)



### 3.5 Scrambled Images (page 55)

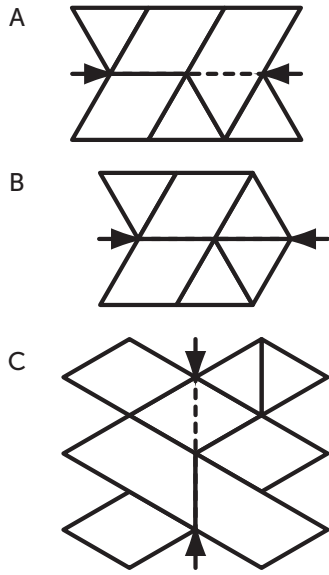
Check students' work.

### 3.6 The Flip Side (page 57)



If a figure is flipped twice, it looks like the original figure. If a figure is flipped an even number of times, it looks like the original figure. If a figure is flipped an odd number of times, it is the mirror image of the original figure.

### 3.7 The Flip Side One More Time (page 59)



### 3.8 Turn About (page 61)

Answers given on teacher page.

### 3.9 One Good Turn Deserves Another (page 63)

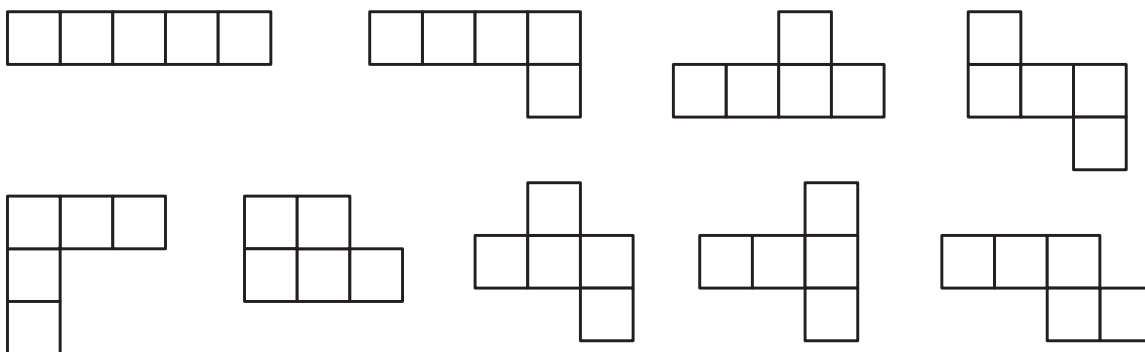
Top 2 figures: Answers given on teacher page.

Bottom 2 figures: 90° rotation; 180° rotation

### 3.10 Double Vision (page 65)

Answers given on teacher page.

### 4.1 Puzzling Pentominoes (page 69)





## 4.2 Green Packages (page 71)

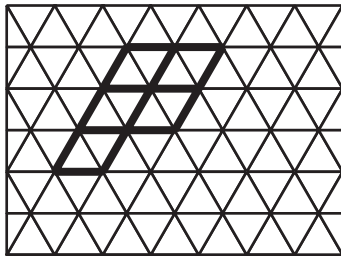
A1 area: 5 triangular units; A2 area: 5 triangular units; Same; The same amount of triangles were used, so the areas are the same.

B1 area: 8 triangular units; B2 area: 8 triangular units; Same; The same amount of triangles were used, so the areas are the same.

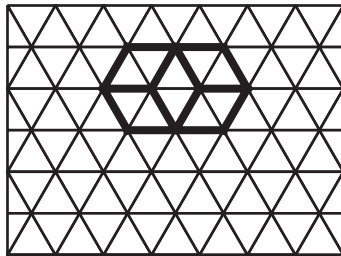
## 4.3 Blue Packages (page 73)

Answers may vary. Sample answers:

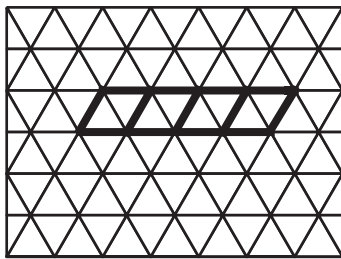
Grid A



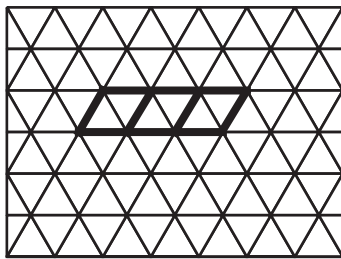
Grid B



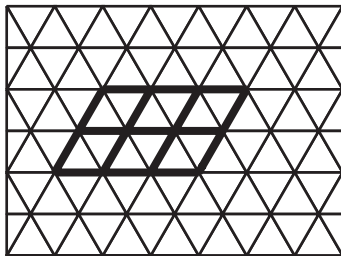
Grid C Area = 8 Perimeter = 10



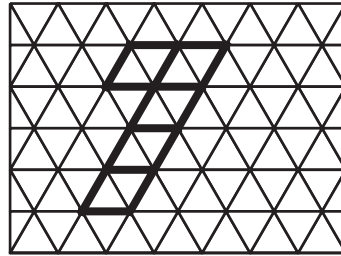
Grid D Area = 6 Perimeter = 8



Grid E Area = 12 Perimeter = 10



Grid F Area = 10 Perimeter = 12



## 4.4 Remodeling (page 75)

Answers may vary. Sample answers:

Triangle: shortest perimeter: 6 units; longest perimeter: 8 units

Blue rhombus: shortest: 8 units; longest: 10 units

Trapezoid: shortest: 10 units; longest: 14 units

## 4.5 Blocks and Corners (page 77)

A: 4, 4, 4

B: 4, 4, 4

C: 4, 4, 4

D: 4, 4, 4

E: 3, 3, 3

F: 6, 6, 6

Mystery Shape: 5, 5, 5

## 4.6 Blocks, Corners, and Intersections (page 79)

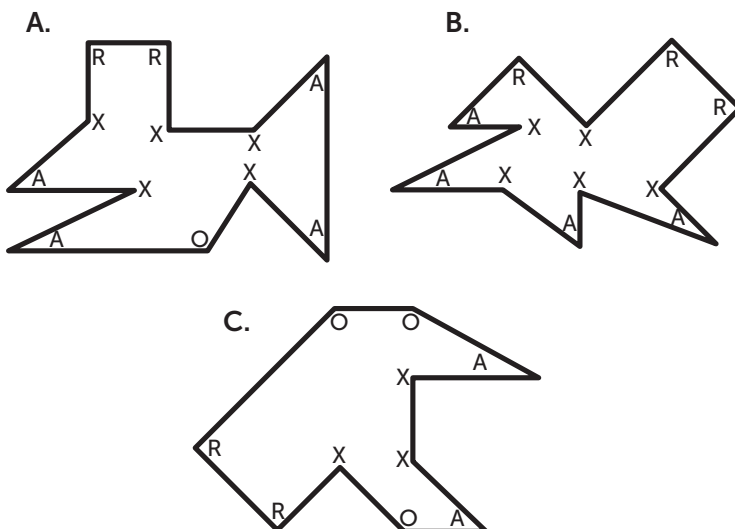
1. Example: Answer is given.
2. Hexagon: All angles are bigger than a right angle.
3. Trapezoid: Angles 1 and 4 are bigger than a right angle. Angles 2 and 3 are smaller than a right angle.
4. Blue rhombus: Angles 1 and 3 are smaller than a right angle. Angles 2 and 4 are bigger than a right angle.
5. Triangle: All angles are smaller than a right angle.
6. Tan rhombus: Angles 1 and 3 are smaller than a right angle. Angles 2 and 4 are bigger than a right angle.

## 4.7 Viewing All Angles (page 81)

### Activity 1:

1, 2, and 3. Answers will vary. Sample answers: trapezoid and blue rhombus; 2 blue rhombuses; hexagon and green triangle.

### Activity 2:



#### 4.8 Forming Flowers (page 83)

1. Answers will vary.
2. 12
3. more blocks
4. Answers will vary.
5. Answers will vary.

#### 4.9 Degree Power (page 85)

1. 90 degrees
2. 30 degrees,  $90 \div 3 = 30$

Angle A:  $60^\circ$

Angle B:  $120^\circ$

Angle C:  $60^\circ$

Angle D:  $120^\circ$

Angle E:  $60^\circ$

Angle F:  $90^\circ$

Angle G:  $150^\circ$

Angle H:  $30^\circ$

Angle K:  $120^\circ$

#### 4.10 Sum Angles (page 87)

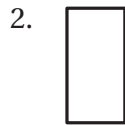
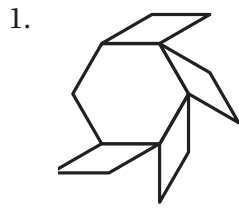
Triangle *ABC*:  $60^\circ, 60^\circ, 60^\circ, 180^\circ$

Blue rhombus *DEFG*:  $60^\circ, 120^\circ, 60^\circ, 120^\circ, 360^\circ$

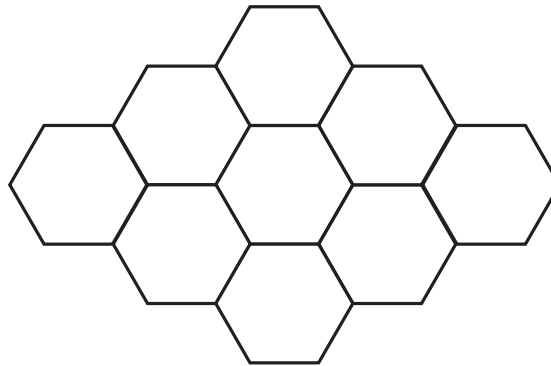
Trapezoid *KLMN*:  $60^\circ, 120^\circ, 120^\circ, 60^\circ$ ; No, the sum is  $360^\circ$ .

Yes, the sum of the measures of the angles of all quadrilaterals is  $360^\circ$ .

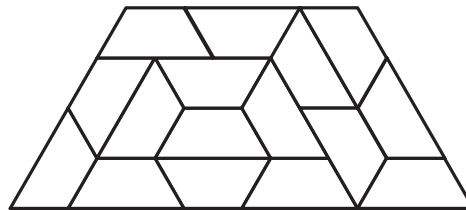
### 5.1 Building Patterns (page 91)



5. Check students' work. The next hexagon in the series should be an arrangement of 9 hexagons. Sample answer:



6. Check students' work. The next trapezoid in the series is a trapezoid made of 16 red blocks. Sample answer:



### 5.2 Triangular Numbers (page 93)

1. A = 1; B = 3; C = 6; D = 10  
 2. E = 15; F = 21  
 3.

Triangle	Number of Green Triangles	Total Number of Green Triangles
A	1	1
B	1 + 2	3
C	1 + 2 + 3	6
D	1 + 2 + 3 + 4	10
E	1 + 2 + 3 + 4 + 5	15
F	1 + 2 + 3 + 4 + 5 + 6	21

4. 10, 15, 21

### 5.3 Square Numbers (page 95)

1.  $A = 1$ ;  $B = 4$ ;  $C = 9$ ;  $D = 16$
2. The number of squares in the next square figure is always the next square number.
3.  $E = 25$ ;  $F = 36$
- 4.


Square	Number of Orange Squares	Total Number of Orange Squares
A	1	1
B	$1 + 3$	4
C	$1 + 3 + 5$	9
D	$1 + 3 + 5 + 7$	16
E	$1 + 3 + 5 + 7 + 9$	25
F	$1 + 3 + 5 + 7 + 9 + 11$	36


5. 16, 25, 36


### 5.4 Triangular or Square Numbers (page 97)

1. tan rhombus:  $(2) = 4$ ,  $(3) = 9$ ,  $(4) = 16$   
 blue rhombus:  $(2) = 4$ ,  $(3) = 9$ ,  $(4) = 16$   
 trapezoid:  $(2) = 4$ ,  $(3) = 9$ ,  $(4) = 16$

- 2.

Shape	Number of Blocks
	
1	1
2	4
3	9
4	16
5	25
6	36

Shape	Number of Blocks
	
1	1
2	4
3	9
4	16
5	25
6	36

Shape	Number of Blocks
	
1	1
2	4
3	9
4	16
5	25
6	36

## 5.5 Hexagons or Triangles (page 99)

1.

Number of Hexagons	Number of Triangles
1	6
2	12
3	18
4	24
5	30
6	36
7	42
8	48
9	54
10	60

- 300 triangles
- 600 triangles
- 1,194 triangles
- To find the number of triangles for any number of hexagons, you would multiply the number of hexagons by 6.
- If  $n$  is the number of hexagons and  $t$  is the number of triangles, then  $t = 6n$ .

## 5.6 Creating Stars (page 101)

Number of Stars	Number of Blue Rhombuses	Number of Triangles
1	4	8
2	8	16
3	12	24
4	16	32
5	20	40
6	24	48
7	28	56
8	32	64
9	36	72
10	40	80

- 8
- 8; 20
- 16; 40
- 200; 196; 800

5. 400; 392; 1,600
6. To find the number of blue rhombuses for any number of stars, you would multiply the number of stars by 4.
7. If  $n$  is the number of stars and  $t$  is the number of triangles, then  $t = 8n$ .

### 5.7 Discovering Formulas (page 103)

1. 12 square units
2. 3
3. 4
4. 12 square units
5. 6
6. 2
7. Yes; Check students' work.
- 8.

Total Area	Rectangle 1		Rectangle 2		Rectangle 3		Rectangle 4	
	Length	Width	Length	Width	Length	Width	Length	Width
12	4	3	6	2	12	1		
18	6	3	9	2	18	1		
24	8	3	6	4	12	2	24	1

9. 24 square units; 24
10. You multiply the length by the width to find the area.
11.  $A = l \times w$

### 5.8 Balances (page 105)

1. 2 blue rhombuses
2. 2 trapezoids
3. 3 blue rhombuses
4. 1 triangle
5. 1 blue rhombus
6. 1 blue rhombus
7. 1 trapezoid
8. 2 blue rhombuses

### 5.9 Grab Bag Mystery (page 107)

Number of Blue Rhombuses	Number of Trapezoids	Number of $\triangle$ Replacing the Blue Rhombuses	Number of $\triangle$ Replacing the Trapezoids	Total Number of Triangles
10	0	20	0	20
9	1	18	3	21
8	2	16	6	22
7	3	14	9	23
6	4	12	12	24
5	5	10	15	25
4	6	8	18	26
3	7	6	21	27

Answer: Dana took 3 blue rhombuses and 7 trapezoids.

- 21
- She would have taken 5 blue rhombuses and 5 trapezoids.

### 5.10 More Grab Bag Fun (page 109)

Number of Hexagons	Number of Trapezoids	Number of $\triangle$ Replacing the Hexagons	Number of $\triangle$ Replacing the Trapezoids	Total Number of Triangles
9	8	54	24	78
10	7	60	21	81
11	6	66	18	84
12	5	72	15	87

Answer: Mary Grace took 12 hexagons and 5 trapezoids.

- If she increased the number of hexagons, she would increase the number of triangles for which she could exchange the blocks. This is because there are twice as many triangles in a hexagon as in a trapezoid.
- $n = 6H + 3T$
- $H + T = 17$



### 6.1 Statistics by Design (1) (page 113)

1. Answers will vary.
2. Check students' work.
3. Check students' work.

### 6.1 Statistics by Design (1) (page 115)

1. Answers will vary.
2. Check students' work.

### 6.2 Design Your Way (page 117)

6 hexagons; 3 trapezoids; 4 blue rhombuses; 7 squares; 1 tan rhombus; 10 triangles.  
Check students' designs made with the given blocks.

### 6.3 Handfuls (page 119)

Answers will vary. Sample answer:  $1/12 + 6/12 + 5/12 = 12/12$

### 6.4 Grab Bag (page 121)

Outcomes	Value in $\triangle_s$	Number of Times Drawn
3 $\triangle$	3	Answers will vary.
2 $\triangle$ , 1 $\diamond$	4	Answers will vary.
2 $\triangle$ , 1 $\square$	5	Answers will vary.
3 $\diamond$	6	Answers will vary.
2 $\diamond$ , 1 $\triangle$	5	Answers will vary.
2 $\diamond$ , 1 $\square$	7	Answers will vary.
3 $\square$	9	Answers will vary.
2 $\square$ , 1 $\triangle$	7	Answers will vary.
2 $\square$ , 1 $\diamond$	8	Answers will vary.
1 $\triangle$ , 1 $\square$ , 1 $\diamond$	6	Answers will vary.

Graph: Check students' work.




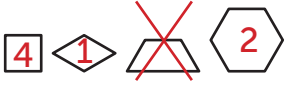








## 6.5 Sampling (page 123)

Answers will vary. Check students' work.

## 6.6 Making Predictions (page 125)

Answers will vary. Check students' work.

## 6.7 All in the Family (page 127)

Rule	Belong	Do Not Belong	Total Belong	Total Do Not Belong
hexagon			2	8
red			3	7
orange or green			4	6
trapezoid			3	7
blue or square			5	5
red or blue			4	6
quadrilateral and a parallelogram			5	5
yellow or a polygon			10	0
orange or a hexagon			6	4
an octagon and yellow			0	10

## 6.8 Targets (page 129)

### Target A

P(S): Answer given.

P(L) = 6/9 or 2/3

**Target B**

$$P(S) = 1/10$$

$$P(L) = 6/10 \text{ or } 3/5$$

**Target C**

$$P(S) = 1/6$$

$$P(L) = 3/6 \text{ or } 1/2$$

**6.9 Hitting the Bulls-Eye (page 131)****Target A**

Solution 1 (using 1 hexagon and 3 triangles):

$$P(S) = 3/9 \text{ or } 1/3$$

$$P(L) = 6/9 \text{ or } 2/3$$

Solution 2 (using 2 trapezoids, 1 blue rhombus, and 1 triangle):

$$P(S) = 1/9$$

$$P(L) = 6/9 \text{ or } 2/3$$

**Target B**

Solution 1 (using 1 hexagon, 1 blue rhombus, 2 triangles):

$$P(S) = 2/10 \text{ or } 1/5$$

$$P(L) = 6/10 \text{ or } 3/5$$

Solution 2 (using 2 trapezoids and 2 blue rhombuses):

$$P(S) = 4/10 \text{ or } 2/5$$

$$P(L) = 6/10 \text{ or } 3/5$$

**Target C**

Solution 1 (using 1 trapezoid, 2 blue rhombuses, and 1 triangle):

$$P(S) = 1/8$$

$$P(L) = 3/8$$

Solution 2 (using 2 trapezoids and 2 triangles):

$$P(S) = 2/8 \text{ or } 1/4$$

$$P(L) = 6/8 \text{ or } 3/4$$

## 6.10 Designing Probability Experiments (page 133)

Check students' work.